

Základní vzorce pro algebraické úpravy

$$\begin{array}{lll}
 (xy)^n = x^n y^n & & \\
 \left(\frac{x}{y}\right)^n = \frac{x^n}{y^n} & \frac{a}{\frac{b}{c}} = \frac{a}{b} \cdot \frac{d}{c} & \log_z a^n = n \log_z a \\
 x^n x^m = x^{n+m} & (a \pm b)^2 = a^2 \pm 2ab + b^2 & \log_z ab = \log_z a + \log_z b \\
 \frac{x^n}{x^m} = x^{n-m} & (a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3 & \log_z \frac{a}{b} = \log_z a - \log_z b \\
 \frac{1}{x^n} = x^{-n} & (a+b)(a-b) = a^2 - b^2 & z^{\log_z a} = a \\
 \sqrt[n]{x} = x^{\frac{1}{n}} & &
 \end{array}$$

Goniometrie

$f(x) \setminus x$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$
$\sin x$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
$\cos x$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
$\operatorname{tg} x$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	—
$\operatorname{cotg} x$	—	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3}$	0

$$\sin^2 x + \cos^2 x = 1$$

$$\operatorname{tg} x = \frac{\sin x}{\cos x}$$

$$\operatorname{cotg} x = \frac{1}{\operatorname{tg} x} = \frac{\cos x}{\sin x}$$

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

Derivace

Funkce	Derivace	Poznámka
k	0	$k \dots$ konstanta
x^n	nx^{n-1}	$n \neq 0$
e^x	e^x	
a^x	$a^x \ln a$	$a > 0$
$\ln x$	$\frac{1}{x}$	
$\log_a x$	$\frac{1}{x \ln a}$	$a \in (0, 1) \cup (1, \infty)$
$\sin x$	$\cos x$	
$\cos x$	$-\sin x$	
$\operatorname{tg} x$	$\frac{1}{\cos^2 x}$	
$\operatorname{cotg} x$	$\frac{-1}{\sin^2 x}$	

$$(f(x) \pm g(x))' = f'(x) \pm g'(x)$$

$$(k f(x))' = k f'(x), \quad k \dots \text{konst.}$$

$$(f(x) \cdot g(x))' = f'(x)g(x) + f(x)g'(x)$$

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)}, \quad g(x) \neq 0$$

$$[f(g(x))]' = f'(g(x)) \cdot g'(x)$$

Primitivní funkce

Primitivní funkce	Poznámka
$\int k \, dx = kx + c$	$k \dots$ konst.
$\int x^n \, dx = \frac{x^{n+1}}{n+1} + c$	$n \neq -1$
$\int e^x \, dx = e^x + c$	
$\int \sin x \, dx = -\cos x + c$	
$\int \cos x \, dx = \sin x + c$	
$\int \frac{1}{x} \, dx = \ln x + c$	
$\int \frac{1}{\cos^2 x} \, dx = \operatorname{tg} x + c$	
$\int \frac{-1}{\sin^2 x} \, dx = \operatorname{cotg} x + c$	

$$\int (f(x) \pm g(x)) \, dx = \int f(x) \, dx \pm \int g(x) \, dx$$

$$\int (k f(x)) \, dx = k \int f(x) \, dx, \quad k \dots \text{konst.}$$

$$\int f(x) \cdot g'(x) \, dx = f(x)g(x) - \int f'(x)g(x) \, dx$$

$$\int f(g(x))g'(x) \, dx = \int f(t) \, dt, \quad g(x) = t, \quad g'(x) \, dx = dt$$